

# Pre-class Warm-up

Consider the problem:

Find the entry in row 2 column 3 of the matrix product

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{bmatrix} \begin{bmatrix} 1 & 0 & -1 \\ -1 & 2 & 1 \end{bmatrix}$$

Here's the question I shall ask you today:

Find someone else who can interview about this.

Is that person able to do this calculation?

Answer:

a. Yes

b. No

- There is a 10 minute quiz tomorrow in your discussion session. You may use a single sheet of handwritten notes.
- Have you had problems getting the Canvas site to work? What doesn't work?

2.1

## How to understand functions of several variables

We learn:

More generally,  $D \subseteq \mathbb{R}^n$   
 is an open subset  
 $f: D \rightarrow \mathbb{R}^m$   $f(D)$  is the range

- How to recognize  $n$  and  $m$  for a function  $f: \mathbb{R}^n \rightarrow \mathbb{R}^m$
- Domain, range, target or codomain
- Describing a function by its graph
- Describing a function by its level sets = contour lines.
- Describing a function by sections
- What some standard functions look like: paraboloids, saddle points.

What are  $n$  and  $m$  in the following functions  $f: \mathbb{R}^n \rightarrow \mathbb{R}^m$ ?

What are the domain and range?

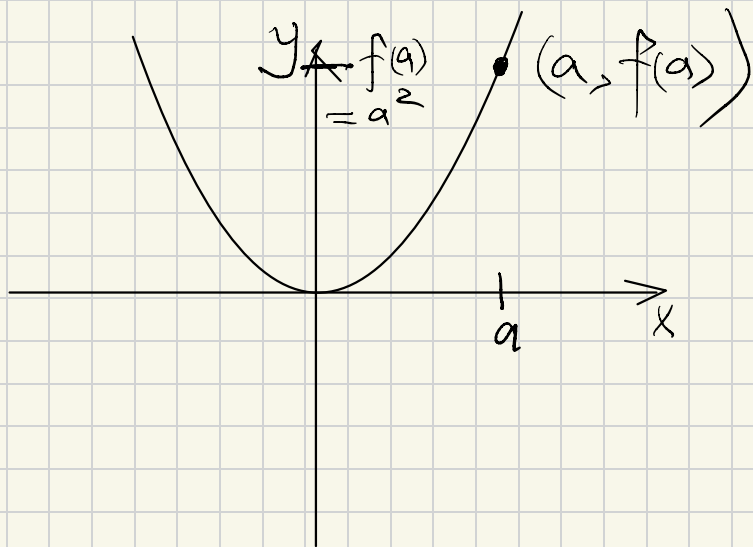
a.  $f(s,t) = (1,2,3) + s(0,-1,1) + t(1,0,2)$

$f: \mathbb{R}^2 \rightarrow \mathbb{R}^3$   
 domain target or codomain  
 $n=2$   $m=3$   
 the range is a plane

b.  $f(s) = (1,2,3) + s(0,-1,1)$

- ?  $n = 1$  and  $m = 1$
- ?  $n = 3$  and  $m = 1$
- ?  $n = 1$  and  $m = 3$  ✓

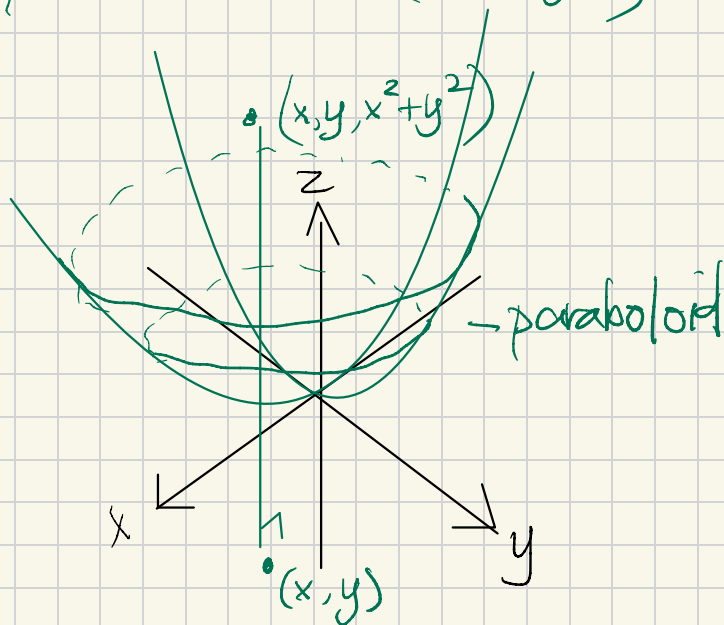
The graph of  $f(x) = x^2$ .



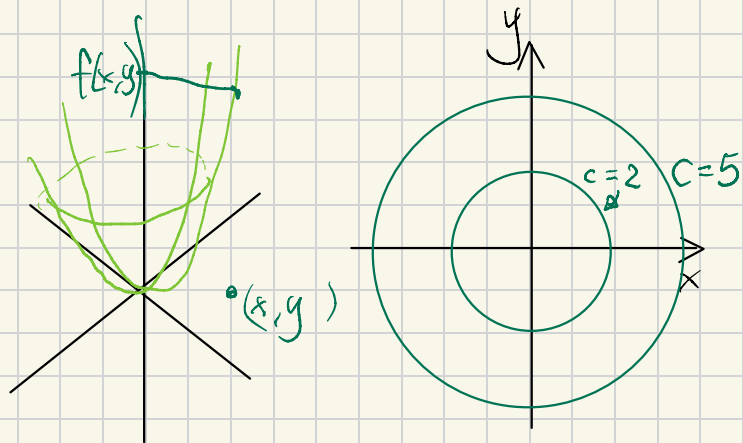
$f: \mathbb{R}^2 \rightarrow \mathbb{R}$   
The graph of  $f(x,y) = x^2 + y^2$

is the set of points  $(x,y,f(x,y))$   
in  $\mathbb{R}^3$

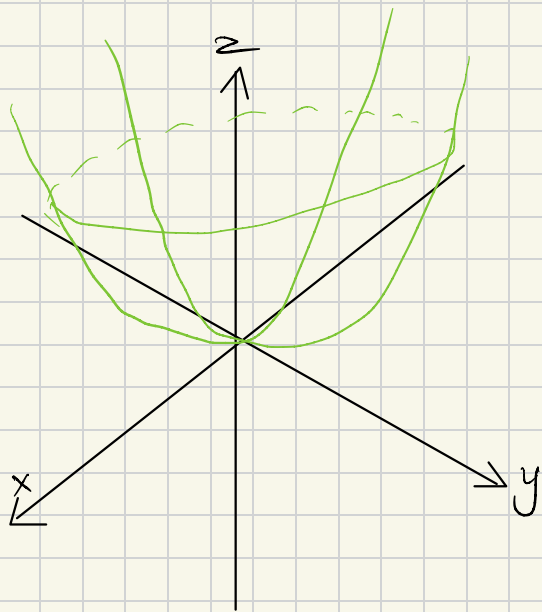
When  $y=0$  we get  $(x, 0, x^2)$   
If  $x=0$  we get  $(0, y, y^2)$



The level sets of  $f(x,y) = x^2 + y^2$  are sets in the domain  $\mathbb{R}^2$  where  $f(x,y) = c$  is constant.



Sections of  $f(x,y) = x^2 + y^2$  are the intersections of the graph with vertical planes.

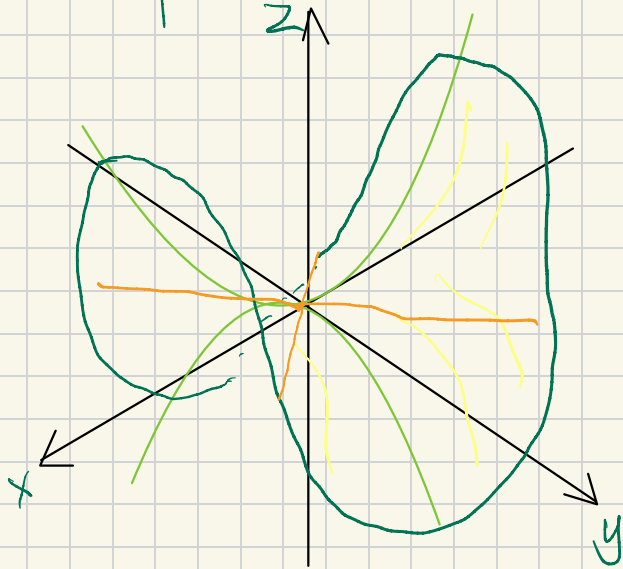


$$f(x,y) = x^2 - y^2$$

Put  $y=0$  : up parabola

$x=0$  : down parabola

saddle point:



Level sets:

